

#1

Let  $x = \text{Chris}$  and  $y = \text{Kim}$ . If Kim painted 10 more than twice the number that Chris painted, then:

$$y = 2x + 10$$

And if they painted 100 boards together, then:

$$x + y = 100$$

Now substitute the first equation into the second.

$$x + (2x + 10) = 100$$

$$3x + 10 = 100$$

(D)

---

#2

Let  $h$  stand for the number of hours. Machine one prints 600 papers an hour. Therefore:

$$\text{Machine 1} \rightarrow 600h$$

Machine two can print 800 each hour but doesn't begin printing until 2 hours after the first machine. Therefore:

$$\text{Machine 2} \rightarrow 800(h-2)$$

Together they must print 15,000 copies, so:

$$600h + 800(h-2) = 15,000$$

$$600h + 800h - 1600 = 15,000$$

$$\frac{1400h}{1400} = \frac{16,600}{1400}$$

$$h = 11.9$$

Equation:  $600h + 800(h-2) = 15,000$       Hours: 11.9

#3

A2A

The area must be less than 65 ft<sup>2</sup>.

$$(base)(height) < 65$$

$$(2x+3)(5) < 65$$

$$10x + 15 < 65$$

$$-15 \qquad -15$$

$$\frac{10x}{10} < \frac{50}{10}$$

$$x < 5$$

(D)

#4

Let  $x$  = pounds of hot dogs and  $y$  = packages of chicken wings. There are two clues given. One involves money and one does not, so you should make two inequalities.

Inequality 1:  $4x + 7y < 42$

Inequality 2:  $x \geq 5$

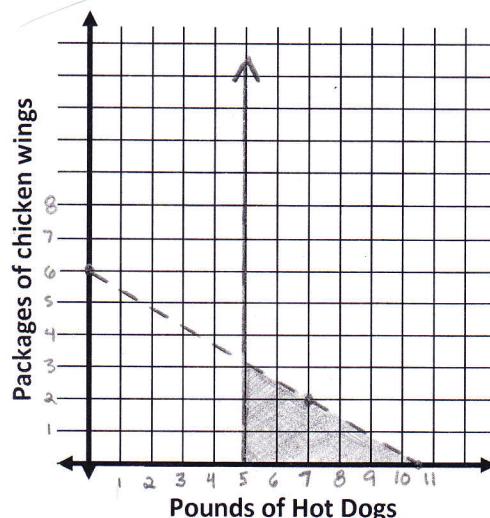
Inequality 1 will be easier to graph in slope-intercept form:

$$4x + 7y < 42$$

$$-4x \qquad -4x$$

$$\frac{7y}{7} < \frac{-4x + 42}{7}$$

$$y < -\frac{4}{7}x + 6$$



Any point in the shaded region is a solution, so just pick two.

For example: (7, 1) and (6, 2)

#5

You can model the situation with an exponential function.

$$B = 5(3)^t$$

↑ initial amount      ↑ growth factor      ↗ increments of 12 hours

Since 48 hours is 4 sets of 12 hours, use  $t=4$ .

$$B = 5(3)^4$$

$B = 405$

To find out how long it takes to have 800 bacteria, let  $B=800$  and solve for  $t$ .

$$\frac{800}{5} = \frac{5(3)^t}{5}$$

$$160 = 3^t$$

Now use "guess and check" to find  $t$ .

Since  $3^4 = 81$  and  $3^5 = 243$ ,  $t$  is between 4 and 5.

Keep testing values between 4 and 5 and you will see that:

$$t \approx 4.62$$

Since  $t$  represents sets of 12 hours, you must multiply by 12.

$$12(4.62) = 55.4 \text{ hours}$$

#6

Since W has the greatest power of 10 in its distance, it is the farthest. Z has the smallest power of 10 so it is the closest. Of the remaining two, Y must be the farthest since 2.279 is greater than 1.496.

(B)

W, Y, X, Z

#7

For  $a^2 - a$  to be negative,  $a^2$  would have to be smaller than  $a$ , which is only true (for positive numbers) when  $a$  is a fraction.

$$0 < a < 1$$

#8

Step 1: Take care of the exponent on the second set of parentheses.

$$(3x^2y^{-5})(-2x\cancel{y^3})^2$$

You must square everything in the parentheses.

$$(3x^2y^{-5})(4x^2y^6)$$

Step 2: Multiply the two terms together.

$$(3x^2y^{-5})(4x^2\cancel{y^6})$$

$$12x^4y$$

#9

A2A

Step 1: Combine the coefficients and the contents of the  $\sqrt{\phantom{x}}$ 's by multiplying.

$$\overbrace{3\sqrt{24} \cdot 4\sqrt{8}} = 12\sqrt{192}$$

Step 2: Simplify the  $\sqrt{\phantom{x}}$ .

$$\begin{array}{c} 12\sqrt{192} \\ \diagdown \quad \diagup \\ 3 \quad 64 \\ \diagdown \quad \diagup \\ 8 \quad 8 \end{array}$$

$$12 \cdot 8\sqrt{3}$$

$$96\sqrt{3}$$

#10

Simply substitute the values into the expression and follow the proper order of operations.

$$\left[ \frac{(-2)(\frac{1}{2}) - (-2)(5)^2}{5 - 2} \right]^2$$

$$\left[ \frac{-1 - (-2)(25)}{7} \right]^2$$

$$\left[ \frac{-1 - (-50)}{7} \right]^2$$

$$\left[ \frac{49}{7} \right]^2$$

$$[7]^2$$

$$49$$

#11

A2A

Finding the domain means figuring out what values of  $x$  can be used in the function. In this case, note that you may only square root a number greater than or equal to zero. Therefore:

$$\begin{aligned} 3x - 6 &\geq 0 \\ +6 & \quad +6 \\ \frac{3x}{3} &\geq \frac{6}{3} \\ x &\geq 2 \end{aligned}$$

(C)

#12

A (True) - Yes, the graph continues indefinitely from left to right.

B (NOT TRUE) - The graph's highest point has a  $y$ -value of 5, so it does not continue up towards  $\infty$ .

C (True) - You can see on the graph that  $f(x)$  crosses the  $x$ -axis at -8 and 2.

D (True) - Yes,  $f(x)$  crosses the  $y$ -axis at 2.

#13

If the diameter triples every day, the function is of the form:

$$f(x) = I(3)^x$$

↑ # of days  
 initial amount

The only graph that represents an increasing exponential function is:

(A)

#14 To find  $f(2)$  you must substitute 2 for  $x$  in the function.

$$f(2) = \frac{3(2)}{(2)^2 - 1}$$

$$= \frac{6}{4-1}$$

$$= \frac{6}{3}$$

$$= \textcircled{2}$$

#15 If  $g(x) = 4$ , then:

$$4 = \frac{9}{10-x}$$

Solve for  $x$ :

~~$4 = \frac{9}{10-x}$~~

$$40 - 4x = 9$$

$$-40 \qquad \qquad -40$$

$$\frac{-4x}{-4} = \frac{-31}{-4}$$

$$x = \frac{31}{4}$$

#16 In an exponential function, each term is multiplied by a particular number to get the next term. Look at the table to find that multiplier.

$x$	$y$
0	3
1	6
2	r

$\downarrow * 2$   
 $\downarrow * 2$

Since 3 is doubled to become 6, the multiplier is 2. Now just double 6:

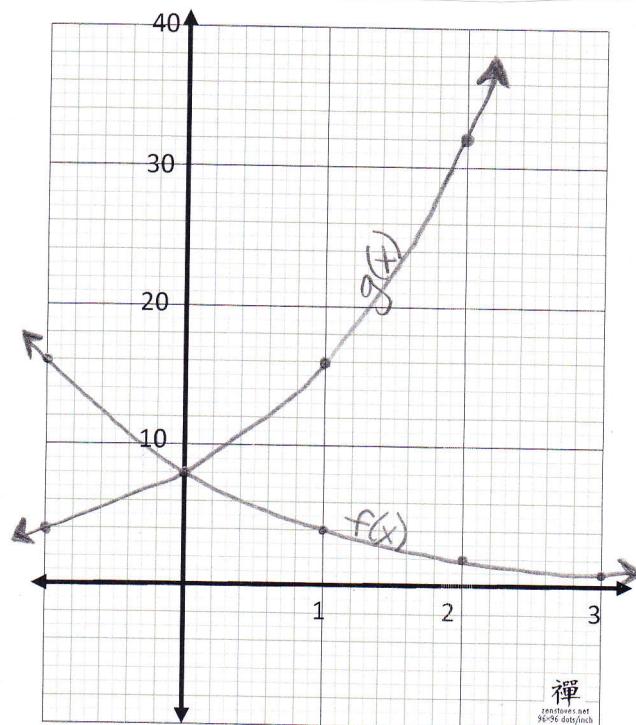
$$r = 6 \cdot 2 = 12$$

(C)

#17

A&amp;A

$x$	$f(x)$ $8(\frac{1}{2})^x$	$g(x)$ $8(2)^x$
-2	32	2
-1	16	4
0	8	8
1	4	16
2	2	32
3	1	64



#18

Use the following compound interest formula:

$$A = P(1 + \frac{r}{n})^{nt}$$

$$A = 2000 \left(1 + \frac{0.04}{2}\right)^{(2)(5)}$$

$$A = 2000 (1 + .02)^{10}$$

$$A = 2000(1.02)^{10}$$

$$A = 2437.99$$

$\left. \begin{array}{l} A = \text{balance after } t \text{ years} \\ P = \text{original amount} \\ r = \text{annual interest rate (as decimal)} \\ n = \# \text{ times compounded annually} \\ t = \text{time in years} \end{array} \right\}$

(C)

#19

4, 7, 10, 13...

To get each term, you add 3 to the term before it.

$$a(0) = 4 \quad a(n+1) = a(n) + 3$$

#20

Isolate h:

A2A

$$2 \cdot A = \frac{h}{2} (b_1 + b_2) \cdot 2$$

$$\frac{2A}{b_1 + b_2} = \frac{h(b_1 + b_2)}{b_1 + b_2}$$

$$h = \frac{2A}{b_1 + b_2}$$